

## ANALISIS DE RELACION Y CORRELACION

Los análisis se realizarán sobre las variables cuantitativas, ya que Stat Graphics no hace el análisis, estudio y graficas de las variables cualitativas. Por lo tanto se tomaran como variables dependientes e independientes, solo aquellas que se pueden ingresar en el sistema, como numéricas (las de caracter no pueden ser analizadas).

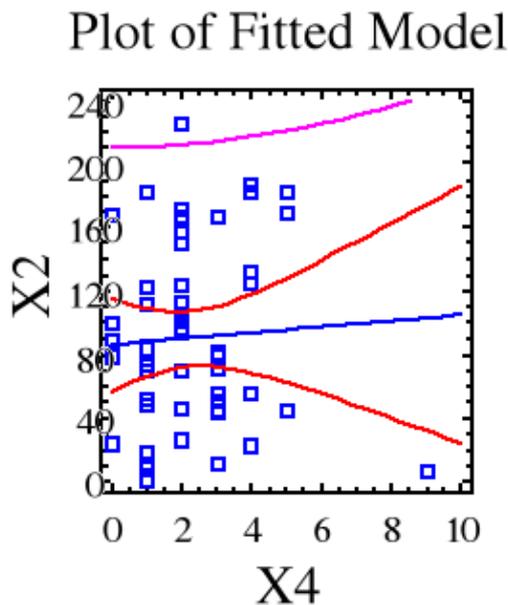
Regresión para pronóstico de corte transversal.

Tipo de Regresión: Simple

- **Variable dependiente: X4 (Número de cursos de educación continua terminados)**
- **Variable Independiente: X2 (Número de horas extra)**

Variable independiente X4 (Eje X)

Variable dependiente X2 (Eje Y)



Ecuación del modelo lineal:  $X2 = 85.7147 + 1.90585X4$

De la cual se deduce: Que el intercepto con el eje Y es 85.7147 y que cada vez que se incrementa en una unidad el número de cursos de educación continua terminados, aumenta en un 1.90585 las horas extras trabajadas.

1. COEFICIENTE DE CORRELACION:  $r = \sqrt{R^2} = 0.05370561$

Como la pendiente es positiva, el coeficiente de correlación también es positivo.

Existe una relación de 0.0536071 entre las variables, la cual es una relación mas bien débil.

2. COEFICIENTE DE DETERMINACIÓN:  $R^2 = 0.00288435$  O  $0.288435\%$

El número de cursos de educación continua, determinan el número de horas extra que trabajan los empleados en un  $0.002874$ , por lo que se vé lo determina muy poco

3. ESTIMACIÓN DE LA VARIANZA DE ERRORES:  $Se^2 = SCE/n-2$   $Se = 1.69363$

### CONTRASTES– INTERVALOS DE CONFIANZA

" "

$$Y = B_0 + B_1 X_i$$

La pendiente mide el grado de inclinación y la relación entre las dos variables.

$$S^2 B_1 = Se^2 / ( \sum X_i^2 - (n \cdot \bar{X}^2) )$$

$$= 0.0000001$$

$$S B_1 = 0.000380$$

$$1 - \alpha = 95\% = 5\%$$

$$t_{0.025; 48} = 2.0106$$

$$LI = 1.90585 - (2.016 \cdot 0.000380) = 1.1.905084$$

$$LS = 1.90585 + (2.016 \cdot 0.000380) = 1.906616$$

$$1.905084 < B_1 < 1.906616$$

### PRUEBAS DE HIPÓTESIS

$$H_0 : B = 0$$

$$H_1 : B \neq 0$$

Rechaza si:  $t_c < -t_{\alpha/2}$  y  $t_c > t_{\alpha/2}$

"

$$t_c = B_1 - B_0 / S_{b1}$$

$$t_c = 1.90585 - 0 / 0.000380$$

$$t_c = 5013.3787$$

$$t_{0.025, 48} = 2.0106$$

$$5013.3787 > 2.0106$$

Rechaza H0. Acepta H1

- **Variable independiente: X2 (Número de horas extra) (Eje X)**
- **Variable dependiente: X4 (Número de cursos de educación continua terminados) (Eje Y)**

Ecuación del modelo lineal :  $X_2=85.7147+1.90585X_4$

De la cual se deduce: Que el intercepto con el eje Y es 85.7147 y que cada vez que se incrementa en una unidad las horas extra , aumenta en un 1.90585 el número de cursos de educación continua terminados.

$X_2$  = Horas extra (Variable independiente : X)

$X_4$  = Cursos de educación continua terminados (Variable dependiente : Y)

1. COEFICIENTE DE CORRELACION: :  $r = R^2$

=0.0537061

Como la pendiente es positiva, el coeficiente de correlación también es positivo.

Existe una relación de 0.0537061 entre las variables, la cual es una relación mas bien débil.

2. COEFICIENTE DE DETERMINACIÓN:  $R^2 = 0.00288435$

El número de horas extra que trabajan los empleados, determinan la cantidad de cursos de educación continua en un 0.002884, por lo que se vé lo determina muy poco

3. ESTIMACIÓN DE LA VARIANZA DE ERRORES:  $Se^2 = SCE/n-2$   $Se = 60.1012$

### CONTRASTES- INTERVALOS DE CONFIANZA

" "

$Y = B_0 + B_1 X_i$

La pendiente mide el grado de inclinación y la relación entre las dos variables.

$S^2_{B_1} = Se^2 / ( \sum X_i^2 - (n \cdot \bar{X}^2) )$

=0.283698

$S_{B_1} = 0.532633$

$1 - \alpha = 95\% = 5\%$

$t_{0.025; 48} = 2.016$

$LI = 1.90585 - (2.016 \cdot 0.532633) = 0.832062$

$LS = 1.90585 + (2.016 \cdot 0.532633) = 2.979638$

0.832062 < B1 < 2.979638

## **PRUEBAS DE HIPÓTESIS**

H0 : B = 0

H1: B ≠ 0

Rechaza si:  $t_c < -t_{/2}$  y  $t_c > t_{/2}$

" "

$t_c = \frac{B_1 - B_0}{S_{b1}}$

$t_c = \frac{1.90585 - 0}{0.532633}$

$t_c = 3.578167$

$t_{0.025, 48} = 2.0106$

$3.578167 > 2.0106$

Rechaza H0. Acepta H1

## **ANÁLISIS DE UNA VARIABLE (INDEPENDIENTE)**

Stat Graphics unicamente hace el análisis de variables cuantitativas, por eso tomaremos como variables independientes solo tomaremos a las variables cuantitativas.

### **1. Variable Independiente: X2 (Horas extra)**

(Cursos de educación continua...)

**VARIABLE INDEPENDIENTE X4**

**TRABAJO DE ESTADÍSTICA**

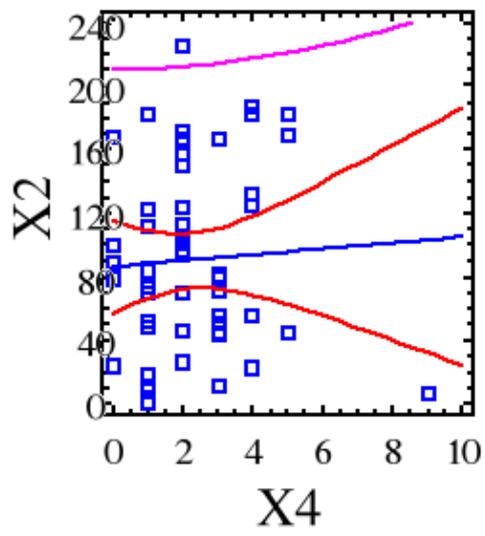
**FECHA: NOVIEMBRE 3 DEL 2000**

**MATERIA: ESTADÍSTICA**

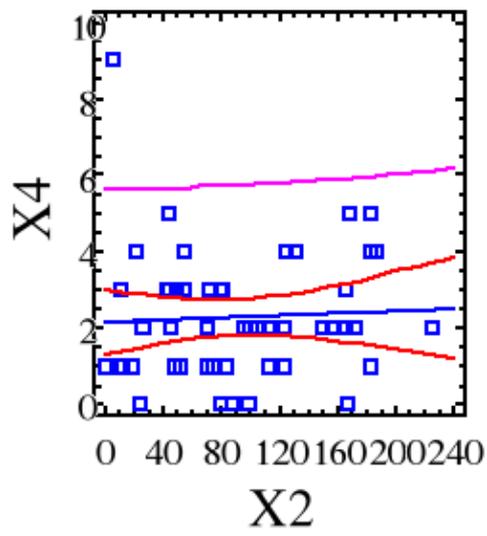
**UNIVERSIDAD EAFIT**

**MEDELLIN**

Plot of Fitted Model



Plot of Fitted Model



## Summary Statistics for X2

Count = 50  
Average = 90,06  
Variance = 3548,67  
Standard deviation = 59,5707  
Minimum = 0,0  
Maximum = 225,0  
Range = 225,0  
Std. skewness = 1,02431  
Std. kurtosis = -1,32

### The StatAdvisor

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This table shows summary statistics for X2. It includes measures of central tendency, measures of variability, and measures of shape. Of particular interest here are the standardized skewness and standardized kurtosis, which can be used to determine whether the sample comes from a normal distribution. Values of these statistics outside the range of -2 to +2 indicate significant departures from normality, which would tend to invalidate any statistical test regarding the standard deviation. In this case, the standardized skewness value is within the range expected for data from a normal distribution. The standardized kurtosis value is within the range expected for data from a normal distribution.

### Analysis Summary

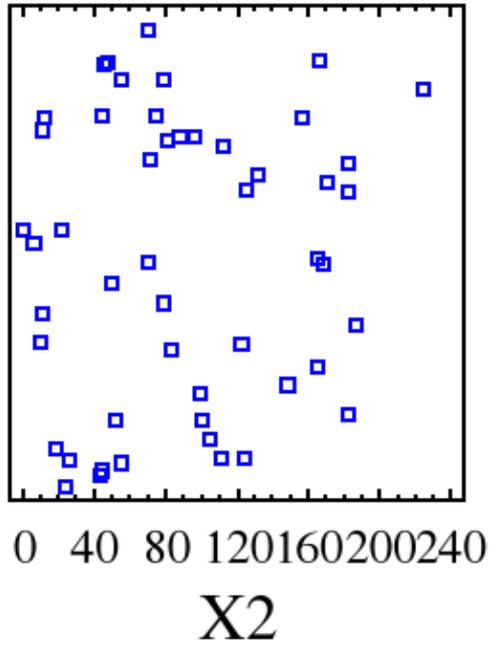
Data variable: X2

50 values ranging from 0,0 to 225,0

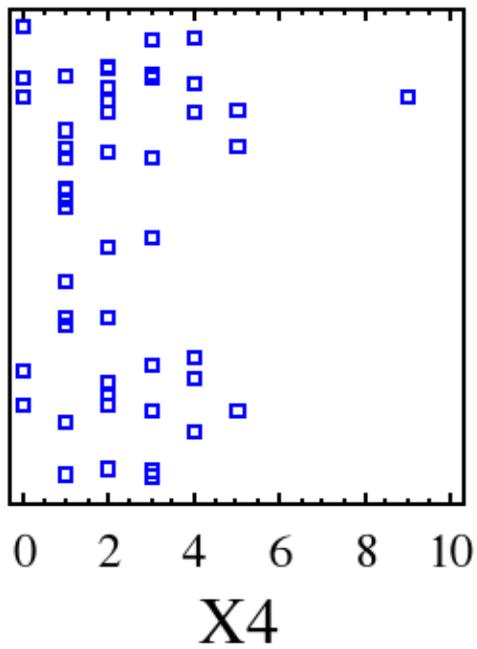
### The StatAdvisor

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This procedure is designed to summarize a single sample of data. It will calculate various statistics and graphs. Also included in the procedure are confidence intervals and hypothesis tests. Use the Tabular Options and Graphical Options buttons on the analysis toolbar to access these different procedures.

Scatterplot for X2



Scatterplot for X4



## Analysis Summary

Data variable: X4

50 values ranging from 0,0 to 9,0

### The StatAdvisor

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This procedure is designed to summarize a single sample of data. It will calculate various statistics and graphs. Also included in the procedure are confidence intervals and hypothesis tests. Use the Tabular Options and Graphical Options buttons on the analysis toolbar to access these different procedures.

### Summary Statistics for X4

Count = 50  
Average = 2,28  
Variance = 2,81796  
Standard deviation = 1,67868  
Minimum = 0,0  
Maximum = 9,0  
Range = 9,0  
Std. skewness = 4,0335  
Std. kurtosis = 5,57409

### The StatAdvisor

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This table shows summary statistics for X4. It includes measures of central tendency, measures of variability, and measures of shape. Of particular interest here are the standardized skewness and standardized kurtosis, which can be used to determine whether the sample comes from a normal distribution. Values of these statistics outside the range of -2 to +2 indicate significant departures from normality, which would tend to invalidate any statistical test regarding the standard deviation. In this case, the standardized skewness value is not within the range expected for data from a normal distribution. The standardized kurtosis value is not within the range expected for data from a normal distribution.

Regression Analysis - Linear model:  $Y = a + b \cdot X$

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Dependent variable: X2  
Independent variable: X4  
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Parameter	Estimate	Standard Error	T Statistic	P-Value
Intercept	85,7147	14,4303	5,93993	0,0000
Slope	1,90585	5,11467	0,372625	0,7111

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Analysis of Variance

Source	Sum of Squares	Df	Mean Square	F-Ratio	P-Value
Model	501,544	1	501,544	0,14	0,7111
Residual	173383,0	48	3612,15		
Total (Corr.)	173885,0	49			

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Correlation Coefficient = 0,0537061  
R-squared = 0,288435 percent  
Standard Error of Est. = 60,1012

The StatAdvisor

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The output shows the results of fitting a linear model to describe the relationship between X2 and X4. The equation of the fitted model is

$$X2 = 85,7147 + 1,90585 \cdot X4$$

Since the P-value in the ANOVA table is greater or equal to 0.10, there is not a statistically significant relationship between X2 and X4 at the 90% or higher confidence level.

The R-Squared statistic indicates that the model as fitted explains 0,288435% of the variability in X2. The correlation coefficient equals 0,0537061, indicating a relatively weak relationship between the variables. The standard error of the estimate shows the standard deviation of the residuals to be 60,1012. This value can be used to construct prediction limits for new observations by selecting the Forecasts option from the text menu.

Regression Analysis - Linear model:  $Y = a + b \cdot X$

Dependent variable: X4  
 Independent variable: X2

Parameter	Estimate	Standard Error	T Statistic	P-Value
Intercept	2,1437	0,43722	4,90302	0,0000
Slope	0,00151342	0,0040615	0,372625	0,7111

Analysis of Variance

Source	Sum of Squares	Df	Mean Square	F-Ratio	P-Value
Model	0,39827	1	0,39827	0,14	0,7111
Residual	137,682	48	2,86837		
Total (Corr.)	138,08	49			

Correlation Coefficient = 0,0537061  
 R-squared = 0,288435 percent  
 Standard Error of Est. = 1,69363

The StatAdvisor

The output shows the results of fitting a linear model to describe the relationship between X4 and X2. The equation of the fitted model is

$$X4 = 2,1437 + 0,00151342 \cdot X2$$

Since the P-value in the ANOVA table is greater or equal to 0.10, there is not a statistically significant relationship between X4 and X2 at the 90% or higher confidence level.

The R-Squared statistic indicates that the model as fitted explains 0,288435% of the variability in X4. The correlation coefficient equals 0,0537061, indicating a relatively weak relationship between the variables. The standard error of the estimate shows the standard deviation of the residuals to be 1,69363. This value can be used to construct prediction limits for new observations by selecting the Forecasts option from the text menu.